

Algebraic Representation of Functions

1) $f(x) = 3 - x^2$

a) $f(0) = 3$

b) $f(\sqrt{3}) = 0$

c) $f(-2) = -1$

2) $f(x) = \begin{cases} \cos x & x \leq 0 \\ 2x & x > 0 \end{cases}$

a) $f(-\frac{\pi}{4}) = \frac{\sqrt{2}}{2}$ c) $f(1) = 2$

b) $f(0) = 1$

d) $f(a^2) = 2a^2$

3) $f(x) = x^2 - 3x + 2$

a) $f(x+h) = (x+h)^2 - 3(x+h) + 2$
 $= x^2 + 2xh + h^2 - 3x - 3h + 2$

b) $f(x+h) - f(x) = x^2 + 2xh + h^2 - 3x - 3h + 2 - (x^2 - 3x + 2)$
 $= 2xh + h^2 - 3h$

c) $\frac{f(x+h) - f(x)}{h} = \frac{2xh + h^2 - 3h}{h}$

$= \frac{h(2x + h - 3)}{h} = 2x + h - 3$

4) $f(x) = \sin x$ $g(x) = \pi x$

a) $f(g(2)) = \sin(2\pi)$
 $= 0$

b) $g(f(0)) = 0$

c) $g(f(\frac{\pi}{4})) = \pi \left[\frac{\sqrt{2}}{2} \right]$

5) $f(x) = \sqrt{x+2}$ $g(x) = 2x$

a) $f(g(x)) = \sqrt{2x+2}$

b) $g(f(x)) = 2\sqrt{x+2}$

c) $f(f(x)) = \sqrt{\sqrt{x+2} + 2}$

d) $g(g(x)) = 2(2x) = 4x$

6) $f(x) = \begin{cases} x^2 + 2, & x \leq 1 \\ 2x^2 + 2, & x > 1 \end{cases}$

a) $f(-2) = -2$

c) $f(1) = 3$

b) $f(0) = 2$

d) $f(s^2+2) = 2(s^2+2)^2 + 2$
 $= 2(s^4 + 4s^2 + 4) + 2$
 $= 2s^4 + 8s^2 + 10$

$$7) a) y = 2 + \sqrt{x-1}$$

$$D: x-1 \geq 0$$

$$D: x \geq 1 \\ [1, \infty)$$

$$b) y = 4 - x^2$$

$$D: \mathbb{R} \text{ or } (-\infty, \infty)$$

$$c) y = \frac{1}{x-2}$$

$$D: x-2 \neq 0$$

$$D: x \neq 2$$

$$\text{or} \\ (-\infty, 2) \cup (2, \infty)$$

$$d) y = \frac{1}{x^2+3x-4}$$

$$x^2+3x-4 \neq 0$$

$$(x-4)(x+1) \neq 0$$

$$D: x \neq 4 \quad x \neq -1$$

$$\text{or} \\ D: (-\infty, -1) \cup (-1, 4) \cup (4, \infty)$$