

Worksheet Review Trig. Identities (basic)

Date _____ Period _____

Verify each identity.

1)
$$\frac{\tan^2 x - \sec^2 x}{\cos x} = -\sec x$$

2)
$$\tan x + \sec x = \frac{1 + \sin x}{\cos x}$$

3)
$$\frac{\sec x}{\sin^3 x} = \frac{\csc^3 x}{\cos x}$$

$$4) \cos x + \sec x = \frac{\cos^2 x + 1}{\cos x}$$

$$5) \cot^2 x + 1 = \frac{1}{\sin^2 x}$$

$$6) \tan x \csc x \sec x = \tan^2 x + 1$$

$$7) \sin^2 x (\tan^2 x + 1) = \frac{\tan x}{\cot x}$$

Answers to Worksheet Review Trig. Identities (basic) (ID: 1)

1) $\frac{\tan^2 x - \sec^2 x}{\cos x}$

Use $\tan^2 x + 1 = \sec^2 x$

$$-\frac{1}{\cos x}$$

Use $\sec x = \frac{1}{\cos x}$

$$-\sec x$$



3) $\frac{\sec x}{\sin^3 x}$

Use $\csc x = \frac{1}{\sin x}$

$$\csc^3 x \sec x$$

Use $\sec x = \frac{1}{\cos x}$

$$\frac{\csc^3 x}{\cos x}$$



5) $\cot^2 x + 1$

Use $\cot^2 x + 1 = \csc^2 x$

$$\csc^2 x$$

Use $\csc x = \frac{1}{\sin x}$

$$\frac{1}{\sin^2 x}$$



6) $\tan x \csc x \sec x$

Decompose into sine and cosine

$$\frac{\sin x}{\cos x} \cdot \frac{1}{\sin x} \cdot \frac{1}{\cos x}$$

Simplify

$$\frac{1}{\cos^2 x}$$

Use $\sec x = \frac{1}{\cos x}$

$$\sec^2 x$$

Use $\tan^2 x + 1 = \sec^2 x$

$$\tan^2 x + 1$$



2) $\tan x + \sec x$

Decompose into sine and cosine

$$\frac{\sin x}{\cos x} + \frac{1}{\cos x}$$

Simplify

$$\frac{1 + \sin x}{\cos x}$$



4) $\cos x + \sec x$

Decompose into sine and cosine

$$\cos x + \frac{1}{\cos x}$$

Simplify

$$\frac{\cos^2 x + 1}{\cos x}$$



$$7) \sin^2 x(\tan^2 x + 1) \quad \text{Use } \tan^2 x + 1 = \sec^2 x$$

$$\sin^2 x \sec^2 x \quad \text{Use } \sec x = \frac{1}{\cos x}$$

$$\frac{\sin^2 x}{\cos^2 x} \quad \text{Use } \cot x = \frac{\cos x}{\sin x}$$

$$\frac{1}{\cot^2 x} \quad \text{Use } \cot x = \frac{1}{\tan x}$$

$$\frac{\tan x}{\cot x} \quad \blacksquare$$